

## Uncertainty and sensitivity issues in process-based models of carbon and nitrogen cycles in terrestrial ecosystems

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**Abstract:** Many process-based models on carbon (C) and nitrogen (N) cycles have been developed for northern forest ecosystems. These models are widely used to evaluate the long-term decisions in forest management dealing with effects like particulate pollution, productivity and climate change. Regarding climate change, one of the key questions that have sensitive political implications is whether northern forests will sequester atmospheric C or not. Whilst many process-based models have been tested for accuracy by evaluating or validating against observed data, few have dealt with the complexity of the incorporated procedures to estimate uncertainties associated with model predictions or the sensitivity of these predictions to input factors in a systematic, inter-model comparison fashion. In general, models differ in their underlying attempts to match natural complexities with assumed or imposed model structure and process formulations to estimate model parameters, to gather data and to address issues on scope, scale and natural variations. Uncertainties may originate from model structure, estimation of model parameters, data input, representation of natural variation and scaling exercises. Model structure relates to the mathematical representation of the processes modelled and the type of state variables that a model contains. The modelling of partitioning among above- and below-ground C and N pools and the interdependence among these pools remain a major source of uncertainty in model structure and error propagation. Most soil C models use at least three state variables to represent the different types of soil organic matter (SOM). This approach results in creating three artificial SOM pools, assuming that each one contains C compounds with same turnover rate. In reality, SOM consists of many different types of C compounds with widely different turnover rates. Uncertainty in data and parameter estimates are closely linked. Data uncertainties are associated with high variations in estimating forest biomass, productivity and soil organic matter and may be incomplete for model initialization, calibration, validation and sensitivity analysis of generalized predictor models. The scale at which a model is being used also affects the level of uncertainty, as the errors in the prediction of the C and N dynamics differ from the site to the landscape levels and across climatic regions. If the spatial or temporal scale of a model application is changed, additional uncertainty arises from neglecting natural variability in system variables in time and space. Uncertainty issues are also intimately related to model validation and sensitivity analysis. The estimation of uncertainties is needed to inform decision process, in order to detect the possible corridor of development. Uncertainty in this context is an essential measure of quality for stakeholder and decision makers.

**Keywords:** northern forest ecosystems; models; structure process formulations, error propagation, uncertainties, sensitivity analyses

## 1. INTRODUCTION

Process-based models designed to simulate the dynamics of carbon (C) and nitrogen (N) cycles in northern forest ecosystems are increasingly being used in concert with other tools to predict the effects of environmental factors on forest productivity [Mickler et al, 2002; Peng et al, 2002; Sands and Landsberg, 2002; Almeida et al, 2004; Shaw et al 2006] and forest-based C and N pools [Seely et al, 2002; Kurz and Apps, 1999; Karjalainen, 1996]. Among the environmental factors, we include everything from intensive management practices to climate change, from local to global and from hours to centuries, respectively. Policy makers, including the general public, expect that reliable, well-calibrated and -documented process-based models will be at the centre of rational and sustainable forest management policies and planning and prioritization of research efforts, especially those addressing issues of global change. In this context, it is important for policy makers to understand the validity of the model results and uncertainty associated to them. The term uncertainty refers to the simple fact of being unsure of something. In the case of a C and N model users are unsure about the model results. Regardless of a model's pedigree, there will always be some uncertainty associated with its output. The true values in this case can most possibly never be determined and users need to assume the aberration between the model results and the true values as a result of uncertainties in the input factors as well as the process representation in the model. If it is also assumed that the model results are evaluated against measurements from which the true values are unknown because of measurement uncertainties, it is important to know the probability spaces for both measurements and model results in order to interpret the results correctly. All these uncertainties are ultimately related to a lack of knowledge about the system under study and measurement errors of their properties. It is inevitable to communicate the process of uncertainty propagation starting from measurements in order to make model results meaningful for decision support. Pizer [1999] explains that including uncertainty as opposed to ignoring it lead to significantly different conclusions in policy making and encourages more stringent policy, which may result in welfare gains.

## 2. UNCERTAINTY

Different sources of uncertainty are generally recognized in models on C and N cycles in forest ecosystems, and in biological models in general [O'Neil and Rust, 1979; Medlyn et al., 2005]:

- Data uncertainty associated with measurement errors, spatial or temporal scales or errors in estimates.
- Model structure, and lack of understanding of the biological processes;
- The plasticity that is associated with estimating model parameters, due to the general interdependence of model variables and parameters; related to this is the search to determine the least set of independent variables required to span the most important system states and responses from one extreme to another, e.g., from frozen to non frozen, dry to wet, hot to cold, calm to stormy, etc;
- The range of variation associated with each biological system under study.

### 2.1. Uncertainty in measurements

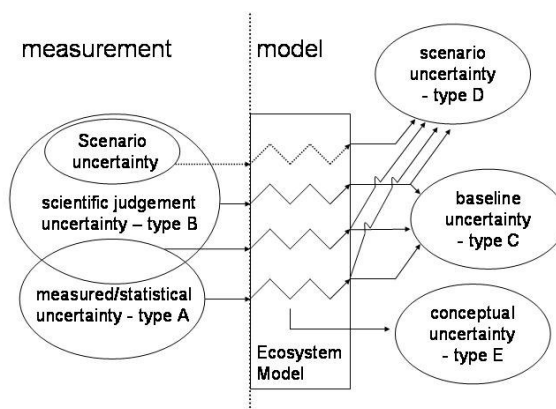
The most comprehensive definition of uncertainty is given by the "Guide to express Uncertainties in Measurements – GUM" [ISO, 1995]: "parameter, associated with the result of a measurement, that characterizes the dispersion of the values that could reasonably be attributed to the measurand". The term parameter may be, for example, a standard deviation (or a given multiple of it), or the half-width of an interval having a stated level of confidence. In this case, uncertainty may be evaluated using a series of measurements and their associated variance (type A, Figure 1) or can be expressed as standard deviation based on expert knowledge or by using all

available sources (type B, Figure 1). With respect to measurements, the GUM refers to the difference between error and uncertainty. Error refers to the imperfection of a measurement due to systematic or random effects in the process of measurement. The random component is caused by variance and can be reduced by an increased number of measurements as we can reduce the systematic component if it occurs from a recognizable process. The uncertainty in the result of a measurement on the other hand arises from the remaining variance in the random component and the uncertainties connected to the correction for systematic effects [ISO, 1995]. If we speak about uncertainty in models it is very important to recognize this concept.

## 2.2 Model uncertainty

The definition of uncertainty in model results can be directly associated to the uncertainty of measurements. However, there are modelling specific components we need to consider. First all models are by definition a simplification of the natural system. Thus it is immanent that uncertainty arises just from the way the model is conceptualized, which is defined as structural uncertainty. C and N models also use parameters in their equations. These internal parameters are associated to model uncertainty and they can have different sources, such as long term experiments (e.g. decomposition constants for soil carbon pools) or laboratory experiments (temperature sensitivity of decomposition), referred to as parameter uncertainty. Both uncertainties refer to the design of the model and can be summarised as conceptual uncertainty (type E, Figure 1) Models are highly dependent on input variables and parameters. Variables are changing over the runtime of a model where parameters are constant, describing the initialisation of the system. As both variables and parameters are model inputs, they are often called input factors in order to distinguish them from internal variables and parameters [Wattenbach et al., 2006].

If the data for input factors are determined by replicative measurements, they can be labeled according to the GUM as type A uncertainty. In many cases the set of type A uncertainty can be influenced by expert judgement (type B uncertainty), which results in the intersection of both sets (e.g., the gapfilling process of flux data is as such a type B uncertainty that influences type A uncertainties in measurements). A subset of type B uncertainty are scenarios. Scenarios are assumptions of future developments based on expert judgement and incorporate the high uncertain element of future developments that cannot be predicted. If we use scenarios in our models, we need to consider it as a separate instance of uncertainty (type D, Figure 1) because it incorporates all elements of uncertainty [Wattenbach et al., 2006].



**Figure 1.** Concept of uncertainty: the measurement uncertainty of type A and/or B are propagated through the model and lead to baseline uncertainty (type C) and scenario uncertainty (type D), where the propagation process is determined by the conceptual uncertainty (type E) (Adapted from Wattenbach et al., 2006).

Many methodologies have been used to better quantify the uncertainty of model parameters. Traditionally, these methodologies include simple trial-and-error calibrations, fitting model calculations with known field data using

linear or non-linear regression techniques and assigning pre-determined parameter values, generated empirically through various means in the laboratory, the greenhouse or the field. For example, Wang et al. [2001] used nonlinear inversion techniques to investigate the number of model parameters that can be resolved from measurements. Braswell et al. [2005] and Knorr and Kattge [2005] used a stochastic inversion technique to derive the probability density functions for the parameters of an ecosystem model from eddy covariance measurements of atmospheric C. Williams et al. [2005] used a time series analysis to reduce parameter uncertainty for the derivation of a simple C transformation model from repeated measurements of C pools and fluxes in a young ponderosa pine stand and Dufrêne et al [2005] used the Monte Carlo technique to estimate uncertainty in net ecosystem exchange by randomly varying key parameters following a normal distribution.

Erroneous parameter assignments can lead to gross over- or under-predictions of forest-based C and N pools. For example, Laiho and Prescott [2004] pointed out that Zimmerman et al. [1995], using an incorrect C/N ratio (of 30) for coarse woody debris in the CENTURY<sup>1</sup> model, greatly overestimated the capability of a forest system to retain N. Prescott et al. [2004] also suggested that models that do not parameterize litter chemistry in great detail may represent long-term rates of leaf litter decay better than those models which do.

The success or failure of a model depends to a large extent on determining whether or not expected model outputs depend on particular values used for model compartment initialization. Models that are structured to be conservative, by strictly following the rules of mass, energy and electrical charge conservation, and by describing transfer processes within the ecosystem by way of simple linear differential or difference equations, lead to an eventual steady-state solution within a constant input-output environment, regardless of the choice of initial conditions. The particular parameter values assigned to such models determine the rate at which the steady state is approached. One important way to test the proper functioning of model parameterization and initialization is to start the model calculations at steady state, and then impose a disturbance pulse, or a series of disturbance pulses (harvesting, fire events, spaced regularly or randomly). This is to see whether the ensuing model calculations will correspond with known system recovery responses, and whether these calculations will eventually return to the initial steady state. In this, the empirical process formulation is crucial, in that each calculation step must feasibly remain within the physically defined solution space. For example, in the hydro-thermal context of C and nutrient cycling, this means that special attention needs to be given to how variations of “independent” variables, such as soil organic matter, texture, coarse fragment content, phase change (water to ice), soil density and wettability, combine deterministically and stochastically to affect subsequent variations in heat and soil moisture flow and retention [Balland and Arp, 2005].

### *2.2.1. Structural uncertainty*

Process-based forest models vary from simple to complex, simulating many different process and feedback mechanisms by integrating ecosystem-based process information on the underlying processes in trees, soil and atmosphere. Simple models often suffer from being too simplistic, but can nevertheless be illustrative and educational in terms of ecosystem thinking. They generally aim at quickly estimating the order of magnitude of C and N quantities associated with particular ecosystem processes, such as C and N uptake and stand-internal C and N allocations. Complex models can, in principle, reproduce the complex dynamics of forest ecosystems in detail. However, their complexity makes their use and evaluation difficult. There is a need to quantify output uncertainty and identify key parameters and variables. The uncertainties are linked: uncertain parameters imply uncertain predictions and uncertainty about the real world implies uncertainty about model structure and parameterization. Because of these linkages, model parameterization, uncertainty analysis, sensitivity analysis, prediction, testing and comparison with other models need to be based on a consistent quantification of uncertainty.

Process-based C and N models are generally referred to as being deterministic or stochastic. These models may be formulated for the steady state (for which inputs equal outputs), or the dynamic situation, where model outcomes depend on time, in relation to time-dependent variations of the model input, and in relation to state-dependent component responses. Models are either based on empirical or theoretical derivations, or a

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<sup>1</sup> <http://www.nrel.colostate.edu/projects/century/nrel.htm>

combination of both (semi-empirical considerations). Process-based modeling is cognizant of the importance of model structure: the number and type of model components are carefully chosen to mimic reality, and to help minimizing the introduction of modeling uncertainties.

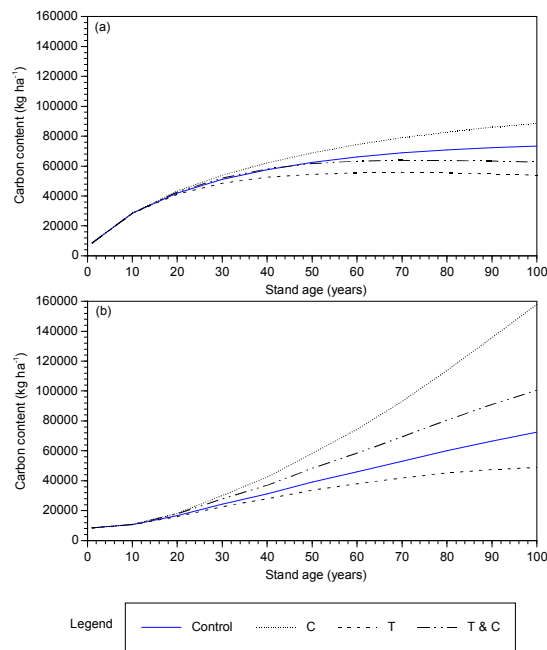
Many problems are generated by model structure alone. Two issues can be related to model structure: (1) mathematical representation of the processes and (2) description of state variables. For example, several types of models can be used to represent the effect of temperature variation on processes, including the  $Q_{10}$  model, the Arrhenius function or other exponential relationships. The degree of uncertainty in the predictions of a model can increase significantly if the relationship representing the effect of temperature on processes is not based on accurate theoretical description [see Kätterer et al., 1998; Thornley and Cannell, 2001; Davidson and Janssens, 2006; Hill et al, 2006]. Most C and N models contain a relatively simple representation of the processes governing soil C and N dynamics, including simplistic parameterization of the partitioning of litter decomposition products between soil organic C and the atmosphere. For example, the description of the mineralization (chemical, physical, and biological turnover) of C and N in forest ecosystems generally addresses three major steps: (1) splitting of the soil organic matter into different fractions, which decompose at different rates, (2) evaluating the robustness of the mineralization coefficients of the adopted fractions, and (3) initializing the model in relation to the fractions [Wander, 2004].

Table 1 gives a cross-section of a number of recent models (or sub-components of models) used to determine litter decomposition rates. The entries in this Table illustrate how the complexity of the C and N modeling approach varies, even in describing a basic process such as forest litter decomposition: the number of C and N components by each model ranged from 5 to 10 (or 6 times the number of cohorts considered in SOMM, starting with 3 C and 3 N organic matter components associated with the decay of single-species leaves). The number of processes considered varied from 5 to 32 and the number of C and N parameters ranged from 7 to 54. The number of additional parameters used for describing the N mineralization process, once the organic matter decomposition process is defined, is particularly interesting: it ranged from 1 to 27.

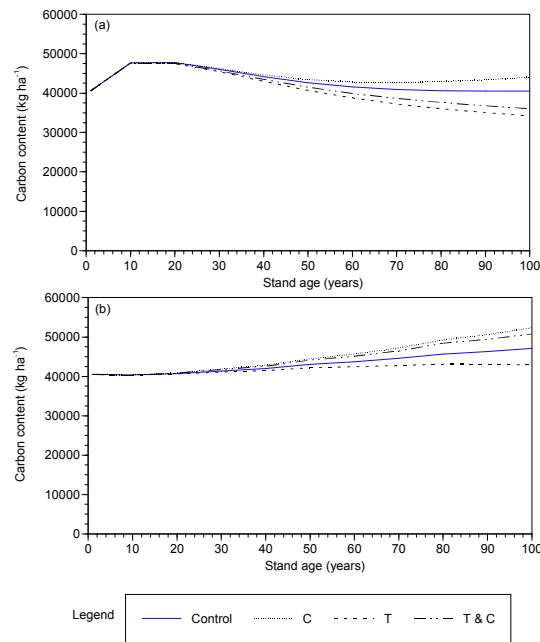
Most soil C models use three state variables to represent different types of soil organic matter (SOM), the active, slow and passive pools. Even though it is assumed that each pool contains C compound types with about the same turnover rate, this approach remains nevertheless conceptual and merely represents an abstraction of reality, which may lead to uncertainty in the predictions (type E, Figure 1) [Davidson and Janssens, 2006]. Also, these conceptual pools do not directly correspond to measurable pools. In reality, SOM contains many types of complex compounds with very different turnover rates and amplitude of reaction to change in temperature [Davidson and Janssen, 2006]. There were many attempts to find relations between model structure and real world either by measuring different decomposition rates of various different soil fractions [Zimmerman et al., 2006] or by restructuring the model pools [e.g., Fang et al, 2005].

Complex models have, in theory, the challenge of being more precise and/or accurate than simple models. This being so, data requirements for the initialization and calibration of complex models need to be tightly controlled, and need to stay within the range of current field experimentation and exploration. The degree of model complexity also needs to be controlled, because this degree affects the overall model transparency and communicability, as well as affordability and practicality. Also, making models more complex can increase their structural uncertainty simply by increasing the number of parameters that are uncertain or affecting the correctness of the description of the processes involved. This can be illustrated by a study conducted by Luckai and Larocque [2002], who compared two complex process-based models, CENTURY and FOREST-BGC, to predict the effect of climate change on C pools in a black spruce (*Picea mariana* [Mill] B.S.P.) forest ecosystem of northwestern Ontario (Figures 2 and 3). For the prediction of the long-term change in C content in the large wood and soil pools, both models predicted relatively close carbon content under scenarios of actual climatic conditions and gradual increase in temperature, even though the pattern of change differed slightly. Substantial differences in C content were obtained when two scenarios of CO<sub>2</sub> increase were simulated. For the effect of gradual CO<sub>2</sub> increase (actual temperature conditions remained unchanged), both models predicted increases in C content relative to actual temperature conditions. However, the increase in large wood C content predicted by

FOREST-BGC was far superior to the increase predicted by CENTURY. The scenario that consisted of a gradual increase in both CO<sub>2</sub> and temperature resulted in widely different patterns. While CENTURY predicted a relatively small decrease in large wood and soil C content, FOREST-BGC predicted an increase. The discrepancies in the results can be explained by differences in the structure of both models. Both models include a description of the above- and below-ground C dynamics. However, CENTURY focuses on the dynamics of litter and soil carbon mineralization and nutrient cycling and FOREST-BGC is based on relatively detailed descriptions of ecophysiological processes, including photosynthesis and respiration. For instance, CENTURY considers several soil carbon pools (active, slow and passive) with specific decomposition rates, while FOREST-BGC considers one carbon pool. Both models also differ in input data. For instance, while CENTURY requires monthly climatic data, FOREST-BGC uses daily climatic data.



**Figure 2.** Carbon content in stems, coarse roots and branches (large wood) predicted by CENTURY (a) and FOREST-BGC (b) under different scenarios of climate change based on CO<sub>2</sub> increase from 350 to 700 ppm (C) and a gradual increase in temperature by 6.1°C (T). The control includes the simulation results when the actual conditions remained unchanged. (Adapted from Luckai and Larocque, 2002).



**Figure 3.** Soil carbon content predicted by CENTURY (a) and FOREST-BGC (b) under different scenarios of climate change based on CO<sub>2</sub> increase from 350 to 700 ppm (C) and a gradual increase in temperature by 6.1°C (T). The control includes the simulation results when the actual conditions remained unchanged. (Adapted from Luckai and Larocque, 2002).

Modellers must carefully consider the trade-off between the potential uncertainty that may result from adding additional variables and parameters and the gain in accuracy by doing so. It may be argued as well that existing models on the C cycle are still in their infancy. It is not evident that modellers involved in the development of process-based models have considered all the tools, including mathematical development, systems analysis and programming, to deal with complexity.

### 2.2.2 Input data uncertainties and natural variation

Data uncertainties are linked to:

- The high spatial and temporal variations associated with forest soil organic matter and corresponding dynamics of above- and below-ground C and N pools. For example, Johnson et al. [2002] noted that soil C measurements from a controlled multi-site harvesting study were highly variable within sites following harvest, but that there was little lasting effect of this variability after 15-16 years. Soil C estimates of an individual pedon are often determined by the combination of measurements of concentration, bulk density, soil depth, and rock content [Homann et al., 1995]; errors in anyone of these can lead to errors in the overall estimate.
- How to determine parameters needed to define, e.g., forest and vegetation type, climate, soil, productivity, and allocation transfers, and to know whether these parameters are truly time and/or state-independent. Calibration parameters are, as a rule, fixed within models. They are usually obtained from other models, derived from theoretical considerations or estimated from the product of combinatorial exercises.

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- Data definitions, sampling procedures, especially those that are vague and open to interpretation, and measurement errors. For example, Gijsman et al. [2002] discussed an existing metadata confusion about determining soil moisture retention in relation to soil bulk density.
- Inadequate sampling strategies, in the context of capturing existing micro- and macro-scale C and N pool variations within forest stands, and across the landscape, at different times of the year. On a regional scale, failure to account for the spatial variation across the landscape and the vertical variation with horizon depth due to microrelief, animal activity, windthrow, litter and coarse woody debris input, human activity and the effect of individual plants on soil microclimate and precipitation chemistry may lead to uncertainty.
- Knowing how errors propagate through the model calculations. For example, soil C and N estimates of individual pedons are generally determined by the combination of measurements of C and N concentrations, soil bulk density, soil depth, and rock content [Homann et al., 1995]; errors in anyone of these add to the overall estimation uncertainties.

By definition, process-based models should be capable of reflecting the range of variation that exists in ecosystems of interest. This is an important issue in forest management. In boreal forest ecosystems, quantifying the range of variation has become a practical goal because forest managers must provide evidence that justifies their proposed use of silviculture (e.g. harvesting, planting, tending) as a stand replacing agent. The range of variation has been defined by Landres et al. [1999] as “the ecological conditions, and the spatial and temporal variation in these conditions, that are relatively unaffected by people within a period of time and geographical area to an expressed goal”. Assuming that reasonable boundaries of time period, geography and anthropogenic influence can be identified, the manager or scientist must then decide which metrics will be used to quantify the range of variation. Common metrics include mean, median, standard deviation, skewness, frequency, spatial arrangement and size and shape distributions [Landres et al., 1999]. The adoption of the range of variation as a guiding principal of forest resource management is well-suited to boreal systems because 1) large, stand replacement natural disturbances continue to dominate in much of the boreal forest and 2) such disturbances may be reasonably emulated by forest harvesting [Haussler and Kneeshaw, 2003].

The boreal forest is a region where climate change is predicted to significantly affect the survival and growth of native species. Consequently, policies and social pressures (e.g. Kyoto Protocol, Certification) may intensify efforts to improve forest C sequestration by reducing “low-value” wood harvesting. However, high prices for crude oil and loss of traditional pulp and paper wood markets may do the opposite by identifying “low-value” forest biomass as a readily available and profitable energy source. Quantifying the range of variation therefore becomes practical as companies and communities charged with forest management have the obligation to provide evidence to justify proposed choices and use of silviculture (e.g. harvesting, planting, tending) as stand-replacing procedures. However, including variables that account for the range of variation increases the number and costs of required model calibrations, even for simple C and N models. An operational definition of the range of variation is also needed, for practical reasons [Ride, 2004].

Structurally, process-based models often include a choice for the user – “stochastic or mean values”. Stochastic runs usually require an estimate of the variation in some aspect of the system of interest. For example, CENTURY has a series of parameters that describe the standard deviation and skewness values for monthly precipitation as main drivers of ecosystem process calculations. This allows the model to vary precipitation, but not air temperature. Another option in CENTURY allows one to write weather files that provide monthly values for temperature and precipitation. However, neither of these options allows for stochasticity in stand replacing events that subsequently affect drivers, such as moisture or temperature, and processes, such as decomposition or photosynthesis.

From a philosophical point of view, it makes sense to build the range of variation into model function. Boreal systems are highly stochastic, the evidence of which can be found in the high level of beta and gamma diversity often reported. From a logistic point of view, however, including variables that account for the range of variation increases the number of required calibration values and subsequently the cost of calibrating even a simple model. Data describing the range of variation is itself hard to come by. More importantly, an operational definition of the range of variation has not been widely adopted [Ride, 2004].



### 2.3 Scenario uncertainty and scaling

The change of scales is an example for input data uncertainty. Models are used on very different scales, e.g., from daily to monthly to annual, and from stand- to catchment- to landscape-levels [Wu et al., 2005]. Data on C and N pools and flows in forest ecosystems, such as those reported and documented in Johnson and Lindberg [1991], are scarce and invaluable, but nevertheless incomplete in several ways: pool sizes and transfers among pools are generally for old growth conditions, and mortality assessments are inconsistent across the sites.

Natural variation, like many other ecological concepts, is scale dependent. For example, at the landscape level, it may be possible (1) to estimate the range of stand compositions and ages and therefore structures, (2) to determine a reasonable range of climatic conditions (mainly minimum and maximum temperatures and precipitation) for timeframes as long as a few rotations (i.e. several hundred years) and (3) to identify the successional pathways that reflect the interaction of (1) and (2). This information could then be used to provide a framework of stand and weather descriptions within which functional characteristics, such as SOM turnover, growth and nutrient cycling, could be modeled. Assuming that we have reasonable mathematical descriptions of key biological, chemical and physical processes – such as photosynthesis and decomposition, weathering and complexation, soil moisture and compaction – we could then “nest” our models one inside of another. This approach implies that the range of variation in the pools and fluxes normally included in process-based models is externally driven (i.e. by weather or disturbance) rather than by internal dynamics.

One example of such a model dealing with the range of variation in scaling issues is the General Ensemble Biogeochemical Modelling System (GEMS), which is used to upscale C and N dynamics from sites to large areas with uncertainty measures [Reiners et al., 2002; Liu et al., 2004a, 2004b; Tan et al., 2005; Liu et al., 2006]. GEMS consists of three major components: one or multiple encapsulated ecosystem biogeochemical models, an automated model parameterization system (AMPS), and an input/output processor (IOP). Plot-scale models such as CENTURY [Parton et al., 1987] and EDCM [Liu et al., 2003] can be encapsulated in GEMS. GEMS uses an ensemble stochastic modeling approach to incorporate the uncertainty and variation in the input databases. Input values for each model run were sampled from their corresponding range of variation spaces usually described by their statistical information (e.g. moments, distribution, etc.). This ensemble approach enables GEMS to quantify the propagation and transformation of uncertainties and errors from inputs to outputs. The expectation and uncertainty of the model output are given as:

$$E[p(X_i)] = \frac{1}{W} \sum_{j=1}^W p(X_{ij}) \quad (1)$$

$$V[p(X_i)] = \frac{1}{W-1} \sum_{j=1}^W (p(X_{ij}) - E[p(X_i)])^2 \quad (2)$$

where  $W$  is the number of ensemble model runs, and  $X_{ij}$  is the vector of EDCM model input values for the  $j$ th simulation of the spatial stratum  $i$  in the study area,  $p$  is a model operator (e.g., CENTURY or EDCM), and  $E$  and  $V$  are the expectation and variance of model ensemble simulations for stratum  $i$ , respectively.

## 3. MODEL VALIDATION

Model validation is an additional source of uncertainty as it compares model results to measurements, which are again associated with uncertainties. Thus the choice of the validation data base determines the accuracy of the model in further ad hoc applications. However, model validation remains a subject of debate and is often used interchangeably with verification [Rykiel, 1996]. Rykiel [1996] differentiated both terms by defining verification as the process aiming at demonstrating the consistency of the logical structure of a model and validation as the process that examines the degree to which a model is accurate relative to the goals desired with respect to its usefulness. Validation does not necessarily consist in demonstrating the logical consistency of causal

relationships underlying a model [Oreskes et al., 1994]. Other authors have argued that validation can never be fully achieved as models, like scientific hypotheses, can only be falsified, not proved, and have promoted the more neutral term “evaluation” for the process of testing the accuracy of a model’s predictions [Smith et al., 1997]. Although model validation can take many forms or include many steps [e.g., Rykiel, 1996], the method that is most commonly used consists in comparing predictions with statistically independent observations. Using both types of data, statistical tests can be performed or indices can be computed. Smith et al. [1997] and Von Gadow and Hui [1999] provide a summary of the indices most commonly used:

$$\text{Mean residual} = (\sum (y_i - \hat{y}_i) / n) \quad (3)$$

$$\text{Root mean square error} = (\sqrt{\sum (y_i - \hat{y}_i)^2 / (n - 1 - p)}) \quad (4)$$

Model efficiency =

$$(\sum (y_i - \hat{y}_i)^2 / \sum (y_i - \bar{y}_i)^2) \quad (5)$$

$$\text{Variance ratio} = \sum (\hat{y}_i - \bar{\hat{y}}_i)^2 / \sum (y_i - \bar{y}_i)^2 \quad (6)$$

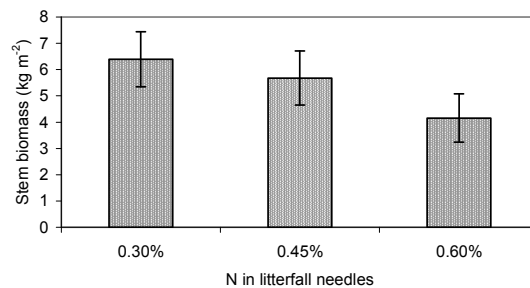
Several examples exist in the literature on the comparison of predictions with observations or field determinations [Smith et al., 1997; Morales et al., 2005], but mostly for traditional empirical growth models in forestry, as part of the procedures used to determine the annual allowable cut within specific forest management units [e.g., Canavan and Ramm, 2000; Smith-Mateja and Ramm, 2002; Lacerte et al., 2004]. In contrast, reports on a systematic validation of C and N cycle models are rare [e.g., deVries et al., 1995; Smith et al., 1997] and needed. The validation of C and N cycle models based on the comparison of predictions and observations has been more problematic than the validation of traditional empirical growth and yield models. The long-term growth and yield data are available for model validation because forest inventories have been conducted by government forest agencies or private industry for many decades. Therefore, process based model testing has been largely based on growth variables, such as annual volume increment [Medlyn et al., 2005]. Although volumetric data can be converted to biomass and C, direct measurements of C and N pools and flows in forest ecosystems have been collected mainly for research purposes and historical datasets are relatively rare. Therefore, it is often difficult to conduct a validation exercise of C and N models based on the comparison of predictions with statistically independent observations.

So, what options exist for the validation of forest-based C and N cycle models? The most logical avenue is the establishment and maintenance of long-term ecological research programs and site installations to generate the data needed for both model formulation and validation. However, these remain extremely costly and don’t receive much political favour in this day and age. One alternative consists in using short-term physiological process measurements [e.g., Davi et al., 2005; Medlyn et al., 2005; Yuste et al., 2005], although care should be given to the long-term behavior of the models in predicting C stocks in vegetation and soils [e.g., Barswell et al., 2005]. Recent technological advances in micrometeorological and physiological instrumentation have been significant, such that it is now possible to collect and analyze hourly, daily, weekly or seasonal data under a variety of forest cover types, experimental scenarios and environmental conditions at relatively low cost. The data from flux tower studies are just now becoming long enough to capture the broad spectrum of climatic and biophysical factors that control the C, water and energy cycles of forest ecosystems. The fundamental value of these measurements derives from their ability to provide multi-annual time series at 30-minute intervals of the net exchanges of CO<sub>2</sub>, water, and energy between a given ecosystem and the atmosphere at a spatial scale that typically ranges between 0.5 and 1 km<sup>2</sup>. The two major component processes of the net flux, ecosystem photosynthesis and respiration data are being collected. Since different ecosystem components can respond differently to climate, multi-annual time series combined with ecosystem component measurements are carried out to separate the responses to inter-annual climate variability. These data are essential for development and validation of process-based models that could be a key part of an integrated C monitoring and prediction system. For example, Medlyn et al. [2005] validated a model of CO<sub>2</sub> exchange using eddy covariance data. Davi et al. [2005] also used data from eddy covariance measurements for the validation of their C and water model, and closely monitored branch and leaf photosynthesis, soil respiration, and sap flow measurement throughout the

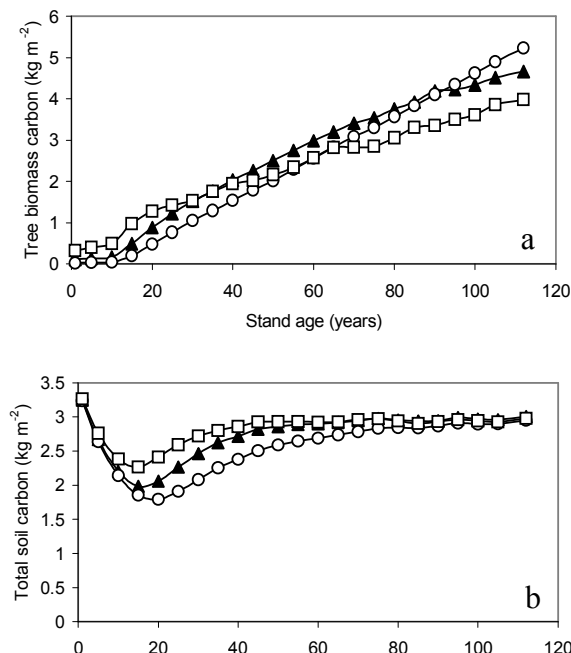
growing season for additional validation purposes. The age factor, the effect of which takes so long to study, can be integrated by using a chrono-sequence approach (using stands of different ages on similar sites as a surrogate for time), which deals with validating C and N models by comparing model output with C and N levels and processes in differently aged forest stands of the same general site conditions. There is also the need to develop new methodologies that are able to integrate the above approaches to allow for model validation at fine and coarse time resolution.

#### 4. SENSITIVITY ANALYSIS

Sensitivity analysis consists in analyzing differences in model response to changes in input factors or parameter values. This exercise is relatively easy when the model contains few parameters, but can become cumbersome for complex process-based models. It is beyond the scope of this paper to review all the different methods that have been used, but one of the best examples of sensitivity analysis for process-based models may be found in Komarov et al. [2003], who carried out the sensitivity analyses for EFIMOD 2. These authors showed that the tree sub-model is highly sensitive to changes in the reallocation of the biomass increment and tree mortality functions while the soil sub-model is sensitive to the proportion and mineralization rate of stable humus in the mineral soil. The model is very sensitive to all N compartments, including the N required for tree growth, N withdrawal from senescent needles, soil N and N deposition from the atmosphere. For example, the prediction of stem biomass is sensitive to the N concentration in needles after abscission (Figure 4), reflecting the degree to which the plant (tree) controls growth by retention and internal N reallocation [Nambiar and Fife, 1991]. However, although uncertainty surrounds initial stand density (often unknown), modelled soil C and N and tree stem C (major source of carbon input to the soil sub-model) are not very sensitive to initial stand density (Figure 5). This type of uncertainty associated with sensitivity analysis could be addressed more thoroughly in the future by including Monte Carlo simulations. Very few examples of this type of integration for carbon cycle models exist. [e.g., Roxburgh and Davies, 2006]. One of the likely reasons was the computer time required. However, the evolution in computer technology is such that this might not be a major issue in a few years.



**Figure 4.** Sensitivity of simulated stem biomass to N content in needles after abscission.



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**Figure 5.** Sensitivity of simulated a) tree biomass carbon, b) total soil carbon and c) total soil nitrogen by EFIMOD 2 to initial stand density

## 5. CONCLUSIONS

Many approaches have been developed and used to calibrate and validate process-based models. Models of the C and N cycles are generally based on sound mathematical representations of the processes involved. However, as previously mentioned, the majority of these models are deterministic. As a consequence, they do not represent adequately the error that may arise from different sources of variation. This is important, as both the C and N cycles (and models thereof) contain many sources of variation. Much can be gained by improving the use of calibration and validation methodologies both for scientists involved in the modelling of these cycles and forest managers who utilize the results.

Upscaling C dynamics from sites to regions is complex and challenging. It requires the characterization of the heterogeneities of critical variables in space and time at the scales that are appropriate with the ecosystem models, and the incorporation of these heterogeneities into field measurements or ecosystem models to estimate the spatial and temporal change of C stocks and fluxes. The success of upscaling depends on a wide range of factors, including the robustness of the ecosystem models across the heterogeneities, necessary supporting spatial databases or relationships that defined the frequency and joint frequency distributions of critical variables, and the right techniques that incorporate these heterogeneities into upscaling processes. Natural and human disturbances of landscape processes (e.g., fires, diseases, droughts, and deforestation), climate change, as well as management practices will play an increasing role in defining the courses of carbon dynamics at local to global scales. Therefore, methods must be developed to characterize the change of these processes in time and space.

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the workshop on uncertainty and sensitivity issues in models of carbon and nitrogen cycles in northern forest ecosystems.

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**Table 1.** Examples of models used for estimating rate of forest litter decomposition.

Model name	Reference	Predicted variables	Initialization variables	Predictor variables	Compartment number	Compartment type	Flows	Parameters	Comments
SOMM	Chertov and Komarov 1997	C and N remaining	Initial C, N, ash content	Annual, monthly or daily soil moisture and temperature estimates	3x C, 3x N; (x represents number of cohorts considered)	C & N litter, fermentation and humus cohorts (leaves, roots, coarse woody debris, etc)	7C, 7N	58 C, 3N	Parameters common across locations, initialized by species (cohort); C/N ratios prescribed per compartment
CENTURY	Parton et al. 1987	C and N remaining	Initial C, N, C/N ratios, lignin	Monthly precipitation and air temperature estimates	5 C, 5 N	Structural, metabolic, active, slow and passive C & N compartments	13 C, 13 N	20 C, 5 N	Parameters common across locations; initialized by species
CANDY	Franco et. al. 1995	C and N remaining	Initial C, N	Monthly or daily soil moisture and temperature estimates	3 C, 3 N	Active, metabolic and stable C & N compartments	3 C, 3 N	5 C, 1 N, + 2 climate parameters (differs from original)	Parameters common across locations; decomposition not species specific
DOCMOD	Currie and Aber 1997	C and N remaining; dissolved organic C and N	Initial C, N, by compartment	Annual actual evapotranspiration estimates	5 C, 5 N	Lignin-cellulose, unprotected cellulose, extractives, microbial and humus C & N compartments	11 C, 10 N	17 C, 4 N	Parameters common across locations; C/N of humus prescribed
FLDM	Zhang et. al. 2006	Mass, C and N remaining	Initial mass, C, N; initial ash and acid and non-acid hydrolyzable fractions, or lignin fraction	January & July air temperatures and annual precipitation, by year; or monthly or daily soil moisture and temperature estimates	3 mass, 2 N	Fast C; slow and very slow C & N compartments	3 C, 2 N	11C, 1 N	Parameters common across locations; CIDET calibrated; C/N ratios process determined
DECOMP	Wallman et al. 2006	CO <sub>2</sub> , soluble compounds, C remaining	Mass, chemical constituents of the soil organic matter (e.g., lignin, holocellulose)	Soil temperature, soil moisture, field capacity, wilting point, potential evapotranspiration, precipitation	4 C, 1 soil solution	Cellulose, lignin easily decomposable and resistant C, cellulose, soil solution	9 C, 9 Water	24 C, 8 water	Very detailed description of the chemistry. Remains to be tested for different sites