

# Relaxor-like Behavior and Structure Features of $\text{Bi}_2\text{Ti}_2\text{O}_7$ Pyrochlore Single Crystals

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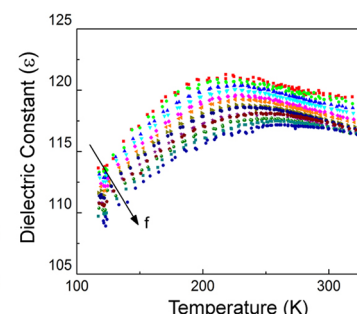
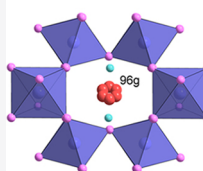


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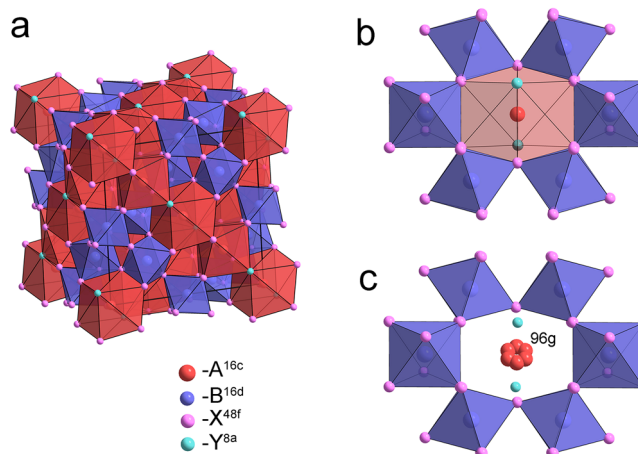
Supporting Information

**ABSTRACT:** By slow cooling of the melt, large  $\text{Bi}_2\text{Ti}_2\text{O}_7$  single crystals with a composition close to stoichiometric were grown. No traces of impurity phases were found on the X-ray diffraction patterns. A structural model with the space group  $Fd\bar{3}m$  and displacive disorder in Bi-sublattice was proposed based on X-ray single crystal diffraction data. The dielectric properties of  $\text{Bi}_2\text{Ti}_2\text{O}_7$  single crystals as a function of temperature at different frequencies were studied for the first time. As in the case of ceramic samples, a step-like frequency-dependent anomaly was detected at a temperature of about 220 K at a frequency of 1 kHz. It was found that attempts to describe the dielectric relaxation using the Arrhenius equation do not lead to physically significant values of the fitting parameters. However, the relaxation behavior is well described by the empirical Vogel–Fulcher relation, which is typical for many dipole and spin glasses, as well as relaxor ferroelectrics. Based on the value of fitting parameters,  $\text{Bi}_2\text{Ti}_2\text{O}_7$  occupies an intermediate position between the canonical relaxor  $\text{PbMg}_{1/3}\text{Nb}_{2/3}\text{O}_3$  on one hand and lead-free weakly coupled relaxors based on  $\text{BaTiO}_3$  on the other one. Possible mechanisms of the observed relaxor-like behavior of the  $\text{Bi}_2\text{Ti}_2\text{O}_7$  single crystal are discussed in terms of correlated hopping of bismuth cations and geometric frustration of the pyrochlore lattice.



## 1. INTRODUCTION

Bismuth titanate  $\text{Bi}_2\text{Ti}_2\text{O}_7$  is a pyrochlore-type compound, first synthesized in the 1960s,<sup>1,2</sup> and has attracted a remarkable amount of researcher attention due to its unusual dielectric and photocatalytic properties.<sup>3–8</sup> The combination of the relatively high dielectric constant ( $\epsilon \sim 100$ ), low dielectric loss, and low sintering temperature makes the title compound a promising material for using in multilayer ceramic capacitors, in storage capacitors of dynamic random access memory (DRAM), and as alternative gate insulating layers in advanced metal oxide semiconductor (MOS) transistors.<sup>9,10</sup> The temperature dependence  $\epsilon$  of  $\text{Bi}_2\text{Ti}_2\text{O}_7$  is characterized by a step-like frequency-dependent anomaly at  $T \sim 200$  K, which was associated with a ferroelectric phase transition in some earlier studies.<sup>11–13</sup> However, later it was shown that  $\text{Bi}_2\text{Ti}_2\text{O}_7$  is a linear dielectric, and the step-like frequency-dependent anomaly is not associated with a ferroelectric phase transition.<sup>8</sup> A specific feature of the  $\text{Bi}_2\text{Ti}_2\text{O}_7$  crystal structure is the disordered displacement of  $\text{Bi}^{3+}$  cations with a lone-electron pair from the Wyckoff position 16c (Figure 1a,b) of the idealized cubic pyrochlore to the Wyckoff position 96g (Figure 1c) or 96h (with a 6-fold decrease in their occupancy), which is also characteristic of other Bi-containing pyrochlores.<sup>14–16</sup> Temperature-activated hopping of bismuth cations between six symmetrically equivalent positions can cause a step-like frequency-dependent anomaly according to some investigations.<sup>17,18</sup> A similar mechanism was previously proposed to

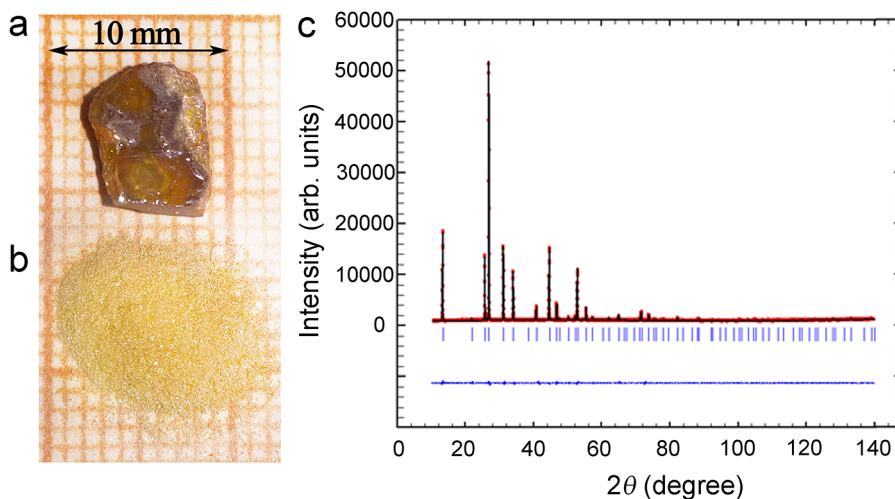


**Figure 1.** (a) Structure of an idealized cubic pyrochlore with the formula  $\text{A}^{16\text{c}}\text{B}^{16\text{d}}\text{X}^{48\text{f}}\text{Y}^{8\text{a}}$  and with space group  $Fd\bar{3}m$ . (b) Local environment of the atom  $\text{A}^{16\text{c}}$  in the structure of idealized cubic pyrochlore. (c) Local environment of the atom  $\text{Bi}^{96\text{g}}$  in the structure of  $\text{Bi}_2\text{Ti}_2\text{O}_7$  according to our experimental data.

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**Figure 2.** (a) Single crystal and (b) powder of  $\text{Bi}_2\text{Ti}_2\text{O}_7$ . (c) X-ray powder diffraction patterns for  $\text{Bi}_2\text{Ti}_2\text{O}_7$ . Observed X-ray data is given in red with the calculated pattern given in black. The difference between observed and calculated patterns is given in blue. The allowed peak positions are marked by the blue ticks.

explain dielectric relaxation in another Bi-containing pyrochlore  $\text{Bi}_{1.5}\text{Zn}_{0.92}\text{Nb}_{1.5}\text{O}_{6.92}$  ( $\text{Bi}_{1.5}\text{Zn}_{1.0}\text{Nb}_{1.5}\text{O}_7$ )<sup>19</sup> and confirmed by comparing the results of dielectric measurements and IR spectroscopy.<sup>20,21</sup>

In the case of  $\text{Bi}_2\text{Ti}_2\text{O}_7$  ceramics, the relaxation process (step-like frequency-dependent anomaly) was described using the Arrhenius equation with low attempt jump frequency ( $\sim 1$  MHz), which was associated with space charge polarization, but not with displacive disorder.<sup>7</sup> However, the manifestation of extrinsic effects, in particular, space charge polarization, is an integral part of the dielectric properties study of ceramic materials.<sup>22–24</sup> In addition, obtaining pure and high-density  $\text{Bi}_2\text{Ti}_2\text{O}_7$  ceramic samples is a complex technological task due to the low temperature stability of the pyrochlore structure, which, according to Hector et al, is associated with a large ratio of ionic radii of  $\text{Bi}^{3+}$  and  $\text{Ti}^{4+}$  cations (1.93).<sup>15</sup> As a result, an increase in the annealing temperature by only 10 °C from the optimum value leads to the appearance of a significant amount ( $\sim 19\%$ ) of the  $\text{Bi}_4\text{Ti}_3\text{O}_{12}$  impurity phase.<sup>15</sup> The latter compound is a well-known high-temperature ferroelectric with a structure of the Aurivillius phase.<sup>25–29</sup> The presence of the  $\text{Bi}_4\text{Ti}_3\text{O}_{12}$  impurity phase determines the visible “ferroelectric” properties of  $\text{Bi}_2\text{Ti}_2\text{O}_7$  ceramics.<sup>8,30</sup>

The reasons that the off-centering tendency of the  $\text{Bi}^{3+}$  cations with a lone-electron pair in Bi-containing pyrochlores do not lead to long-range ordering of local distortions, as observed in many ferroelectric perovskites, are discussed from the point of view of the geometric frustration concept.<sup>31,32</sup> However, unlike many other Bi-containing pyrochlores exhibiting a temperature- and frequency-dependent dielectric relaxation (for example,  $\text{Bi}_{1.5}\text{Zn}_{1.0}\text{Nb}_{1.5}\text{O}_7$ <sup>21</sup> or  $\text{Bi}_{1.56}\text{Fe}_{1.09}\text{Nb}_{1.15}\text{O}_7$ <sup>33</sup>), there is no chemical disorder (disordered distribution of various ions at sites of equivalent crystallographic positions) in  $\text{Bi}_2\text{Ti}_2\text{O}_7$ . This allows us to separate the effect of chemical (compositional) disorder, which is characteristic of many relaxor ferroelectrics, from the possible manifestation of the geometric frustration characteristic of cationic sublattices in the structure of cubic pyrochlores. Thus,  $\text{Bi}_2\text{Ti}_2\text{O}_7$  is a good model system for understanding polar phenomena in the bismuth pyrochlores.

A study of the structure and dielectric properties of pure  $\text{Bi}_2\text{Ti}_2\text{O}_7$  single crystals would “shed light” on the origin of step-like frequency-dependent dielectric anomaly at  $T \sim 200$  K, as well as contribute to understanding the fundamental role of geometric frustration in the formation of responses of nonmagnetic materials. However, up to now, there were no reports on the growth of large enough single crystals of  $\text{Bi}_2\text{Ti}_2\text{O}_7$  for dielectric measurements with a composition close to the stoichiometric one. Earlier, Shimada et al.<sup>34</sup> reported the growth of  $\text{Bi}_2\text{Ti}_2\text{O}_7$  crystals from melts containing  $\text{Bi}_2\text{O}_3$ ,  $\text{TiO}_2$ , and  $\text{V}_2\text{O}_5$  with the addition of 10 mol %  $\text{ZnO}$ . However, it was later shown that the composition of the crystals corresponds to the formula  $\text{Bi}_{1.61}\text{Zn}_{0.18}\text{Ti}_{1.94}\text{V}_{0.06}\text{O}_{6.62}$  with the presence of impurities.<sup>35</sup> In this study, we report the growth of impurity-free large single crystals of  $\text{Bi}_2\text{Ti}_2\text{O}_7$  and the results of the study of their structure features by X-ray single crystal diffraction. For the first time, the dielectric properties of  $\text{Bi}_2\text{Ti}_2\text{O}_7$  single crystals were measured, and it was also shown that dielectric relaxation is described by the empirical Vogel–Fulcher law, which is typical for the canonical relaxors.

## 2. EXPERIMENTAL SECTION

**Crystal Growth.** Single crystals were grown using a slow cooling of the melt of a mixture of  $(1-x)\text{Bi}_2\text{O}_3 - x\text{TiO}_2$  with  $x \sim 0.6$  in open yttrium-stabilized zirconium oxide crucibles in air atmosphere. At the same time, mixtures of  $\text{Bi}_2\text{O}_3$  and  $\text{TiO}_2$  oxides (analytical grade of purity, 99.0%) homogenized by grinding in an agate mortar in an ethyl alcohol medium were used as a batch. The size of the particles in the mixture was around 5–10  $\mu\text{m}$ . The batch was placed in a cylindrical crucible with a capacity of 60  $\text{cm}^3$ ; the degree of filling was 80% of its volume. Next, the batch was melted by heating it for 3 h to 1473 K; the melt was kept at this temperature for 1 h, then cooled to 1173 K at the rate of 7.5 K/h, and then cooled to room temperature with the furnace switched off.

The crystallized melt was a conglomerate of both crystals of  $\text{Bi}_2\text{Ti}_2\text{O}_7$  and small plate-like crystals of  $\text{Bi}_4\text{Ti}_3\text{O}_{12}$ . It was possible to distinguish single crystals of the  $\text{Bi}_2\text{Ti}_2\text{O}_7$  isometric habitus with sizes up to  $3 \times 10 \times 10 \text{ mm}^3$  (Figure 2a). The single crystallinity of such samples was confirmed by the results of the registration of diffractograms in  $\theta$ – $2\theta$  geometry from them (see below), on which reflections from only one single crystal were found. The mirror-smooth most-developed face of the crystals coincides with the surface of the crystallized melt and is the (111) crystallographic plane in the

cubic setting. Traces of the impurity phase ( $\text{Bi}_4\text{Ti}_3\text{O}_{12}$  impurity crystals) were present only in a thin layer on the surface of the solidified melt (Supporting Information, Figure S1). After cleaning the surface (for example, by etching it in acid), this peaks were absent. The milled powder obtained from the  $\text{Bi}_2\text{Ti}_2\text{O}_7$  single crystal has a grayish yellow color (Figure 2b), which is also characteristic of the phase-pure samples.<sup>8</sup> Such a diffraction pattern without reflections of the impurity phase is shown in Figure 2c.

**X-ray Single Crystal Diffraction.** The experimental X-ray structural data set for the  $\text{Bi}_2\text{Ti}_2\text{O}_7$  single crystal was obtained on a Bruker SMART APEX II automatic diffractometer equipped with an Oxford Cobra low-temperature cryosystem at a temperature close to room temperature (graphite monochromatic  $\text{Mo K}_\alpha$  radiation,  $\lambda = 0.71073 \text{ \AA}$ ,  $\omega$ -scan,  $T = 290 \text{ K}$ ). Integration of X-ray diffraction peak intensities was carried out using the SAINT v 8.32B software; the SADABS v 2013 program included in the APEXII package<sup>36</sup> was used to take into account the absorption by crystal habitus, the reduction to a uniform scale, and the averaging of the integral intensities of the experimental data. Structural refinements were performed using SHELX-2014 software<sup>37,38</sup> using the XPREP utility to determine the correct space group. The model of crystal structure was refined by full-matrix least-squares over  $F^2 hkl$  with anisotropic thermal parameters for all atoms. The parameters of the X-ray diffraction experiment and the final results of crystal structure refinements are presented in Table 1.

**Table 1. Crystallographic and Experimental Data and Structure Refinement Parameters for a  $\text{Bi}_2\text{Ti}_2\text{O}_7$  Crystal**

Chemical formula	$\text{Bi}_2\text{Ti}_2\text{O}_7$
Molecular weight	625.76
Temperature (K)	290(2)
Crystal size (mm)	$0.245 \times 0.241 \times 0.084$
Crystal system	Cubic
Crystal shape	Triangular prism
Wavelength ( $\text{\AA}$ )	0.71073
Space group	$Fd\bar{3}m$ (No 227)
$a$ ( $\text{\AA}$ )	10.3714(3)
$V$ ( $\text{\AA}^3$ )	1115.6(1)
$Z$	8
Number of measured reflections	7252
Number of independent reflections	246
Number of reflections with $I > 2\sigma(I)$	225 ( $R_{\text{int}} = 0.059$ )
$\theta$ (deg)	$3.402\text{--}44.335$
Absorption coefficient ( $\mu$ ) ( $\text{mm}^{-1}$ )	65.648
Number of specified parameters	16
$R$ ( $I > 2\sigma(I)$ )	0.0522
$wR$ ( $I > 2\sigma(I)$ )	0.1139
GOOF	1.396

**X-ray Powder Diffraction.** The phase identification and purity of the powder prepared from single crystal was checked from the X-ray powder diffraction (XRPD) patterns obtained on a Bruker D8 Advance diffractometer (Vantec position-sensitive detector, Ge-monochromatized  $\text{Cu K}_\beta$  radiation, Bragg–Brentano geometry, DIFFRACT plus software) in the  $2\theta$  range  $5\text{--}140^\circ$  with a step size of  $0.02^\circ$  (counting time was 15 s per step). XRPD patterns (Figure 2) were analyzed with the full-profile Rietveld profile method

implemented in the FULLPROF software.<sup>39</sup> The diffraction peaks were described by a pseudo-Voigt profile function, with a Lorentzian contribution to the Gaussian peak shape. A peak asymmetry correction was made for angles below  $35^\circ$  ( $2\theta$ ). Background intensities were estimated by interpolating between up to 40–50 selected points or described by a polynomial with six coefficients.

The microstructure of the crystals was characterized by a scanning electron microscope (SEM) (JEOL, JSM6510LV).

**Analysis of Chemical Composition.** ICP-AES Jobin-Yvon JY 70 spectrometer was used to determine a real cation composition of single crystals. Crystals were fused with  $\text{LiBO}_2$  and dissolved in  $\text{HNO}_3$ . Ten measurements per sample were made and the average plus standard deviation (SD) values were taken. Typical analytical precision was better than 1% of the measured values. The total amount of impurity cations did not exceed 0.05 at %. According to the elemental analyses done on different crystallites, the metal compositions of  $\text{Bi}_2\text{Ti}_2\text{O}_7$  samples follow, if the sum of the cations is assumed to be 4 (at % Bi, 49.91(3); Ti, 50.09(3)). These values are very close to the expected ratios and permit us to conclude that sample stoichiometry is identical to the nominal case.

**Dielectric Measurement.** Dielectric measurements were carried out using an E7-20 immittance meter (Minsk Scientific Research Instrument Making Institute, Belarus) at electric field frequencies of  $25\text{--}10^6 \text{ Hz}$  in the temperature range  $4.2\text{--}1000 \text{ K}$ . The sample was in the form of a rectangular plate with the sizes of  $4 \times 4 \times 1 \text{ mm}^3$ . The base surface of the sample was covered by the electrodes which were obtained by burning Ag-paste at  $\sim 773 \text{ K}$ . A special measuring cell was used in which the sample was attached to the Pt plates by means of a soft spring. Data on the resistance (Figure S2) were calculated from the data on dielectric permittivity  $\epsilon$  and the tangent of dielectric loss angle  $\tan \delta$  by the formula  $\rho = 1/2\pi f\epsilon\epsilon_0 \tan \delta$ , where  $f$  is the frequency of the measuring field, and  $\epsilon_0$  is electric constant.

The X-ray powder diffraction pattern registered from the sample after these measurements showed that there was no phase decomposition at the stage of this measuring process.

### 3. RESULTS AND DISCUSSION

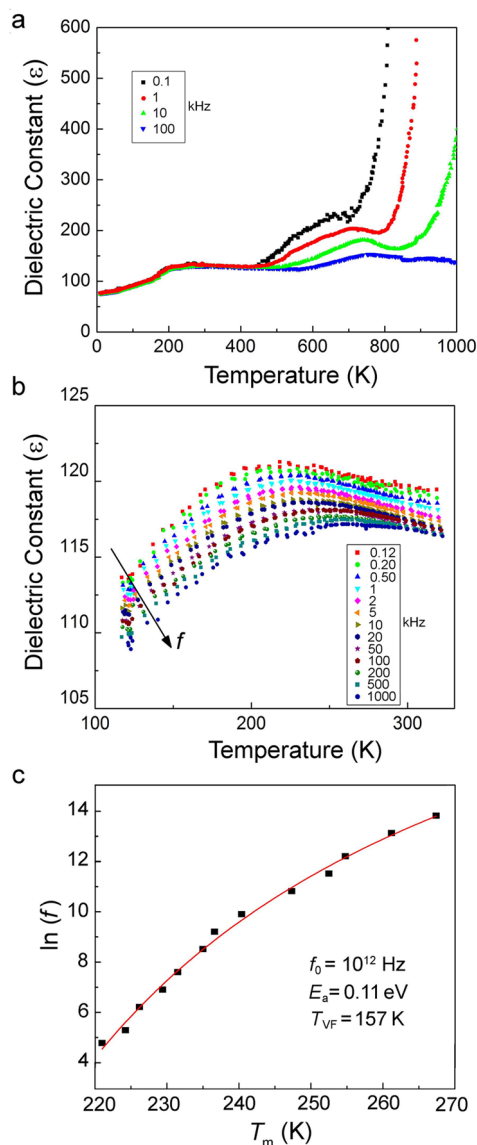
XRD on  $\text{Bi}_2\text{Ti}_2\text{O}_7$  single crystals at room temperature revealed that they retain the cubic pyrochlore structure with space group  $Fd\bar{3}m$  (Table 1). The results of the X-ray diffraction analysis of  $\text{Bi}_2\text{Ti}_2\text{O}_7$  crystals (Table 2) have much in common with the models proposed on the basis of Rietveld refinements of X-ray and neutron powder diffraction data.<sup>15,40</sup> First of all, we found that Bi cations are displaced from the Wyckoff position 16c with local symmetry  $\bar{3}m$  in the  $\{111\}$  plane by  $0.3895 \text{ \AA}$  and occupy the Wyckoff position 96g with local symmetry  $m$ . Note that a similar Wyckoff position for bismuth cations was proposed based on the X-ray powder diffraction study<sup>15</sup> and first-principles calculations.<sup>8</sup> However, in a number of studies, Wyckoff position 96h<sup>40–42</sup> is used for bismuth cations, which is pointed between nearby 48f anions (Wyckoff position 96g shifted to the nearest 48f anion; see Figure 1c).

Since the model of the structure of this compound was proposed earlier, we decided to thoroughly investigate the structural model proposed by Hector and Wiggins (see the table with its structural parameters<sup>15</sup>) and compare with our model. So, let us start our setup with their experimental details.

**Table 2. Atomic Coordinates Occupation Factors and Isotropic Thermal Parameters for  $\text{Bi}_2\text{Ti}_2\text{O}_7$**

atom	Wyckoff position	$x$	$y$	$z$	occupancy	$U_{\text{iso}}$ ( $\text{\AA}^2$ )
Bi	96g	0.0158(4)	0.0158(4)	0.9697(4)	0.1667	0.0191(6)
Ti	16d	0	1/4	3/4	1.000	0.0100(4)
O1	48f	0.1810(6)	−1/8	7/8	1.000	0.0147(9)
O2	8a	−1/8	−1/8	7/8	0.72(10)	0.052(14)





**Figure 3.** (a) Temperature dependences of the dielectric constant measured upon cooling at different frequencies in the  $\text{Bi}_2\text{Ti}_2\text{O}_7$  single crystal. (b) Step-like frequency-dependent anomaly of the  $\text{Bi}_2\text{Ti}_2\text{O}_7$  single crystal. (c) Plots of  $\ln(f)$  vs  $T_m$  and VF relation fitting (red line).

Step-like frequency-dependent anomaly is observed at  $T = 279$  220 K at  $f = 1$  kHz (Figure 3b), which is comparable with 280 previous results obtained on the ceramic samples.<sup>7,8</sup> The 281 maximum values of  $\epsilon$  are 116 (at  $f = 500$  kHz), and  $\tan \delta < 282$  0.01, which is also very close to the results in the indicated 283 works, where  $\epsilon = 115$ .<sup>8</sup> However, we also note the differences: 284 at frequencies less than 10 kHz, no additional anomaly is 285 observed at  $T > 200$  K, as in ref 7. As  $f$  increases, the dielectric 286 maximum temperature ( $T_m$ ) shifts by more than 50 K, and the 287 shape of the step-like frequency-dependent anomaly is 288 smoothed. Attempts to describe the behavior of the  $T_m$  289 frequency dependence using the Arrhenius equation led to 290 physically insignificant values of the attempts frequency to 291 overcome the potential barrier  $f_0 \sim 10^{25}$  (Table 3, Supporting 292 Information, Figure S3). An attempt to isolate two relaxation 293 processes described by Arrhenius equations with different 294 parameters (Table 3, Supporting Information, Figure S4) led 295

217 We used modern single crystal X-ray diffractometer with a  
218 fairly accurate measurement of the structural amplitudes; our  
219 crystal was definitely single-domain. Owing to the cubic  
220 symmetry of  $\text{Bi}_2\text{Ti}_2\text{O}_7$  crystal, a large number of equivalent  
221 reflections was measured, the averaging of which allowed us to  
222 reliably refine the structure by the method of least-squares  
223 (more than 10 reflections per refined parameter). The possible  
224 disadvantages of our experiment include the fact that X-rays  
225 are in principle not particularly sensitive for the determination  
226 of the parameters of the oxygen sublattice in the structures  
227 with heavy cations. We also note that the crystal was not  
228 isometric, which allowed us to estimate the absorption  
229 correction with a certain error.

230 In the case of investigation performed in ref 15, the authors  
231 used the neutron powder diffraction method. Neutrons are  
232 quite sensitive to oxygen, and this allowed them to hope for an  
233 accurate determination of the coordinates and populations of  
234 oxygen. However, their sample was not single crystal, and  
235 moreover, there was an impurity  $\text{Bi}_4\text{Ti}_3\text{O}_{12}$  in the powder,  
236 which probably led to a violation of the stoichiometry of the  
237 studied sample. The Rietveld method which was mainly used  
238 in this research is based on the knowledge of a certain initial  
239 model, which is a significant limitation of the method. In our  
240 case, we obtained a model directly from a set of intensities  
241 without binding it to previously defined structural models.

242 As a result of our crystal structure determination, a  
243 statistically significant structure model was found. The Bi  
244 cation is shifted from a highly symmetric position due to a  
245 lone-electron pair. Regarding oxygen, we tried to add some  
246 kind of disorder, but all attempts did not allow us to make a  
247 certain conclusion because of its weak influence on the  
248 diffraction pattern. So, the question with  $\text{O}_2$  oxygen ordering is  
249 still unanswered. The increased value of the thermal parameter  
250 can be an indicator of disorder, but the position of the split  
251 oxygen can be determined only by difference synthesis maps,  
252 when all previously defined atoms are subtracted. In our  
253 experiment, nothing like  $\text{O}_2$  splitting could be determined, but  
254 it is important to note that for our crystal, the refined  
255 occupation factor of  $\text{O}_2$  is not complete (0.72 (10) instead of  
256 1.0). There is probably a slight oxygen deficiency, but  
257 additional measurements (neutrons, DTA, iodometric titra-  
258 tion) are needed to confirm this conclusion.

259 In the model proposed in ref 15,  $\text{O}_2$  was artificially split. The  
260 effect of this disorder is not evident because the thermal  
261 parameters for these splitting anions are still rather large in  
262 comparison with Bi and Ti. At the same time, all other atoms  
263 of the model<sup>15</sup> are defined (within their accuracy) correctly  
264 and are consistent with ours.

265 Figure 3a shows the temperature dependence of the  
266 dielectric constant ( $\epsilon$ ) for the  $\text{Bi}_2\text{Ti}_2\text{O}_7$  single crystal measured  
267 at different frequencies on cooling. There are two dielectric  
268 anomalies: a strongly relaxing maximum at  $T = 500$ –800 K  
269 and a step-like frequency-dependent anomaly at  $T \approx 200$  K.  
270 The high-temperature anomaly is characterized by a significant  
271 shift in the maximum temperature ( $T_m$ ) (more than 150 K)  
272 with frequency. A similar low-frequency behavior of the  
273 dielectric constant was observed in many oxide dielectrics and  
274 is associated with an increase in conductivity with increasing  
275 temperature and relaxation of the space charge.<sup>22</sup> In our case,  
276 there is also a sharp increase in conductivity at  $T > 500$  K by  
277 more than 3 orders of magnitude (Supporting Information,  
278 Figure S2).

**Table 3. Fitting Parameters of the Arrhenius and Vogel–Fulcher laws for the Bi<sub>2</sub>Ti<sub>2</sub>O<sub>7</sub> Single Crystal**

	$f_0$ (Hz)	$E_a$ (eV)	$T_{VF}$ (K)	$R_{adj}^2$
Arrhenius	$4.5 \times 10^{25}$	1.05	-	0.972
Arrhenius (2)	$5.1 \times 10^{21}$	0.83	-	0.988
	$6.8 \times 10^{30}$	1.27	-	0.991
Vogel–Fulcher	$1 \times 10^{12}$	0.11	157	0.994

to a similar result. However, obtained experimental results are well described (with  $R_{adj}^2 = 0.994$ ,  $R_{adj}$  is the adjusted coefficient of determination) by the empirical Vogel–Fulcher relation (Table 3, Figure 3c)

$$f = f_0 \exp[-E_a/k(T_m - T_{VF})]$$

where  $f_0$  is the attempted frequency to overcome the potential barrier;  $E_a$  is the activation energy;  $k$  is Boltzmann constant,  $T_{VF}$  is the Vogel–Fulcher temperature. In the canonical relaxor PbMg<sub>1/3</sub>Nb<sub>2/3</sub>O<sub>3</sub>, these parameters have a clear physical meaning; in particular,  $T_{VF}$  is associated with the freezing temperature of dipole reorientation dynamics and transition in the non-ergodic relaxor state on cooling.<sup>43</sup> However, as shown by Tagantsev,<sup>44</sup> the Vogel–Fulcher law for the frequency dependences of  $T_m$  (in contrast to the temperature dependences of the relaxation time) can also be observed in systems without freezing the dynamics of the dipoles. Therefore, to establish the real mechanisms of dielectric relaxation in the Bi<sub>2</sub>Ti<sub>2</sub>O<sub>7</sub>, investigation of the temperature dependence of the relaxation time in a wide frequency range, as well as distribution function, is necessary. Nevertheless, using the Vogel–Fulcher law to describe the frequency dependences of  $T_m$  and comparing the corresponding fitting parameters are convenient tools for comparing relaxor-like materials.

In the case of the Bi<sub>2</sub>Ti<sub>2</sub>O<sub>7</sub> single crystals,  $f_0 \sim 10^{12}$  is on the order of phonon frequency and is comparable with the results obtained for other Bi-containing pyrochlores (BZN) from the Arrhenius analysis.<sup>20,21,45</sup> The value of  $E_a = 0.11$  eV is higher than the value determined for the canonical relaxor PbMg<sub>1/3</sub>Nb<sub>2/3</sub>O<sub>3</sub> ( $E_a = 0.76$  eV),<sup>46</sup> but is very close to the parameters of many lead-free relaxors,<sup>47</sup> in particular to  $(1 - x)$  BaTiO<sub>3</sub> –  $x$ BaSnO<sub>3</sub><sup>48</sup> and  $(1 - x)$  BaTiO<sub>3</sub> –  $x$ BaZrO<sub>3</sub><sup>49</sup> at  $x = 0.3$  and  $x = 0.4$ – $0.5$ , respectively. We also note the qualitative similarity of the temperature dependences of the dielectric constant for Bi<sub>2</sub>Ti<sub>2</sub>O<sub>7</sub> single crystals and  $(1 - x)$  BaTiO<sub>3</sub> –  $x$ BiScO<sub>3</sub> solid solutions with  $x = 0.2$ – $0.4$ .<sup>50</sup> However, due to the large values of  $E_a$  ( $\sim 0.25$  eV), as well as high coercive fields and low remanent polarization, the latter were assigned to a weakly coupled relaxor. Thus, Bi<sub>2</sub>Ti<sub>2</sub>O<sub>7</sub> in terms of the fitting parameter  $E_a$  occupies an intermediate position between the canonical relaxor PbMg<sub>1/3</sub>Nb<sub>2/3</sub>O<sub>3</sub> on one hand and lead-free weakly coupled relaxors based on BaTiO<sub>3</sub> on the other.

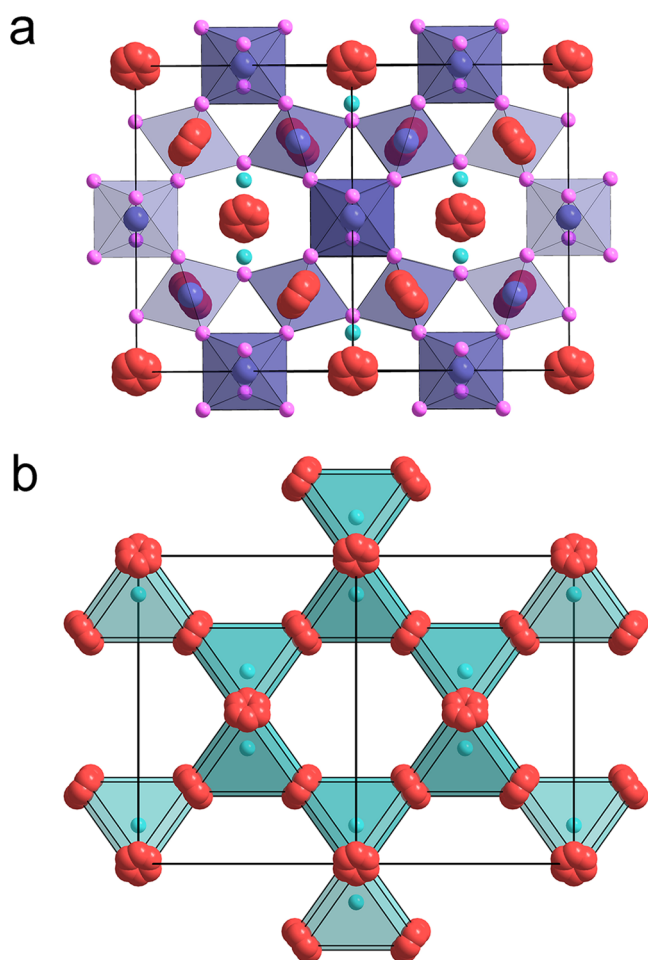
The value of  $T_{VF} = 157$  K is lower than the maximum temperature of the step-like frequency-dependent anomaly by more than 50 K. In the canonical relaxor PbMg<sub>1/3</sub>Nb<sub>2/3</sub>O<sub>3</sub>, the value of  $T_{VF}$  corresponds to the transition temperature from the ergodic to non-ergodic relaxor state upon cooling,<sup>43</sup> wherein the macroscopic structure of PbMg<sub>1/3</sub>Nb<sub>2/3</sub>O<sub>3</sub> remains cubic up to 5 K with decreasing temperature.<sup>51,52</sup> In the case of many other relaxors, for example, PbZn<sub>1/3</sub>Nb<sub>2/3</sub>O<sub>3</sub> and  $(1 - x)$  PbMg<sub>1/3</sub>Nb<sub>2/3</sub>O<sub>3</sub> –  $x$ PbTiO<sub>3</sub> with  $x \sim 0.25$ , a diffuse transition to the ferroelectric phase takes place upon cooling, rather than the transition to the non-ergodic relaxor

state. In this case, the determined value of the  $T_{VF}$  parameter does not have a clear physical meaning, and the dielectric relaxation mechanisms are not associated with the freezing of the dipole dynamics.<sup>53</sup> However, this is accompanied by symmetry lowering of the macroscopic crystal structure, while Bi<sub>2</sub>Ti<sub>2</sub>O<sub>7</sub> (like PbMg<sub>1/3</sub>Nb<sub>2/3</sub>O<sub>3</sub>) is cubic down to low temperatures without undergoing the ferroelectric phase transition.<sup>15</sup>

Note that, despite the very close values of the parameters  $E_a$  and  $f_0$  in Bi<sub>2</sub>Ti<sub>2</sub>O<sub>7</sub> and in Bi<sub>1.5</sub>Zn<sub>1.0</sub>Nb<sub>1.5</sub>O<sub>7</sub> ( $E_a \sim 0.2$  eV,  $f_0 \sim 10^{12}$  Hz<sup>21</sup>), the nature of the manifestation of the dielectric relaxation in them is fundamentally different. For Bi<sub>1.5</sub>Zn<sub>1.0</sub>Nb<sub>1.5</sub>O<sub>7</sub>, the temperature behavior at the low-frequency end of the distribution of Debye relaxation frequencies obeys the Arrhenius law, which implies that the charges hop independently of each other.<sup>54</sup> Attempts to use the Vogel–Fulcher law for Bi<sub>1.5</sub>Zn<sub>1.0</sub>Nb<sub>1.5</sub>O<sub>7</sub> were unsuccessful in the case of films<sup>55</sup> or led to insignificant  $T_{VF} = 0.4$  K in the case of ceramics,<sup>21</sup> confirming the correctness of the Arrhenius law fitting. In Bi<sub>2</sub>Ti<sub>2</sub>O<sub>7</sub>, on the contrary, the  $T_{VF}$  value is significant, and the use of the Arrhenius law cannot lead to physically meaningful fitting parameters (Table 3). This means that the correlation effects between dipoles (or hopping motion) cannot be neglected.

According to the first-principle calculations, bismuth ions hopping between symmetrically equivalent positions separated by an energy barrier of 0.11–0.21 eV are the source of dielectric relaxation in Bi<sub>2</sub>Ti<sub>2</sub>O<sub>7</sub>.<sup>17</sup> Then, taking into account our dielectric spectroscopy data, we can assume the existence of a correlation between the temperature-induced hopping of various bismuth ions. The existence of a correlation between the static displacements of neighboring bismuth atoms was also reported.<sup>41</sup> This work claims that  $\angle \text{Bi–Bi}$  for neighboring displacements has a preference for 180° alignment, which corresponds to zigzag ordering. A similar correlation between Bi-displacements was found in the first-principles study of Bi<sub>2</sub>Ti<sub>2</sub>O<sub>7</sub>.<sup>56</sup> The  $\beta$ -cristoballite-type orientational disorder in the Bi<sub>2</sub>O' substructure was also found in other Bi-containing pyrochlores,<sup>57–59</sup> and it is believed that strongly correlated displacements within Bi<sub>4</sub>O' tetrahedrons affect the manifestation of dielectric properties.<sup>19,57</sup> A recent work notes the universal nature of such displacements within the pyrochlore structure with an emphasis on the manifestation of structural frustration and the lack of ferroelectric behavior in pyrochlores.<sup>60</sup>

It is well-known that cations with a lone pair of electrons, such as Bi<sup>3+</sup> and Pb<sup>2+</sup>, tend to have off-center shifts. Coherent lone pair displacements produce a ferroelectric ground state in the case of textbook compounds PbTiO<sub>3</sub> and Bi<sub>4</sub>Ti<sub>3</sub>O<sub>12</sub> with the structure of perovskite and the Aurivillius phase, respectively. The structure of the idealized cubic pyrochlore  $A^{16c}_2B^{16d}_2X^{48f}_6Y^{8a}_8$  with the space group  $Fd\bar{3}m$  is characterized by the interconnected tetrahedra network formed by atoms at Wyckoff positions 16d and 16c (in Bi<sub>2</sub>Ti<sub>2</sub>O<sub>7</sub>, the bismuth ion is shifted to position 96g (Table 2, Figure 4a)).<sup>61</sup> Such a crystalline structure is frustrated, and if antiferromagnetically coupled magnetic ions are located at the vertices of the tetrahedra, then spin-liquid or spin-glass behavior will be expected.<sup>62,63</sup> If the network of tetrahedra is formed by ions with a lone pair of electrons, then their coherent off-centering distortions are frustrated and the transition to the ferroelectric state is suppressed.<sup>31</sup> By analogy with magnetic systems, the term “charge-ice” was proposed for pyrochlore containing ions



**Figure 4.** (a) Crystal structure of the  $\text{Bi}_2\text{Ti}_2\text{O}_7$  single crystal along the [110] direction at room temperature. Bi atoms and Ti atoms are shown by red and deep blue color, respectively; O1 atoms and O2 atoms are shown by purple and cyan color, respectively. (b) Interconnected tetrahedra network formed by Bi atoms. Only the shortest Bi–Bi distances in tetrahedra are shown.

dielectric relaxation is described by the empirical Vogel–Fulcher relation. Cooling  $\text{PbMg}_{1/3}\text{Nb}_{2/3}\text{O}_3$  below  $T_{\text{VF}}$  leads to the transition to the non-ergodic relaxor state.<sup>43</sup> However, the method used to estimate the dielectric relaxation in  $\text{Bi}_2\text{Ti}_2\text{O}_7$  does not allow us to interpret the physical meaning of the fitting parameters of the Vogel–Fulcher law, in particular,  $T_{\text{VF}}$ . For this reason, the nature of the low-temperature state of  $\text{Bi}_2\text{Ti}_2\text{O}_7$  is unclear and requires further study using methods of broadband dielectric spectroscopy.

#### 4. CONCLUSIONS

Large impurity-free  $\text{Bi}_2\text{Ti}_2\text{O}_7$  single crystals were grown by slow cooling of a melt of a  $\text{Bi}_2\text{O}_3$ – $\text{TiO}_2$  mixture. Using X-ray single crystal diffraction, the  $\text{Bi}_2\text{Ti}_2\text{O}_7$  structure was established at room temperature and its cubic symmetry with the space group  $Fd\bar{3}m$  was confirmed. Bismuth cation is shifted from a highly-symmetry 16c Wyckoff position to a 96g one, which confirms the displacive disorder in the structure of the single crystals. The dielectric properties of  $\text{Bi}_2\text{Ti}_2\text{O}_7$  single crystals were studied for the first time, and it was shown that, as in the case of ceramics, a step-like frequency-dependent anomaly at  $T = 220$  K (at  $f = 1$  kHz) is observed. It was found that attempts to describe the frequency dependence of  $T_{\text{m}}$  for  $\text{Bi}_2\text{Ti}_2\text{O}_7$  single crystals using the Arrhenius equation lead to physically insignificant fitting parameters. However, it was found that frequency dispersion of  $T_{\text{m}}$  is well-described by the empirical Vogel–Fulcher relation, which is typical for many relaxors. By the value of  $E_{\text{a}}$ ,  $\text{Bi}_2\text{Ti}_2\text{O}_7$  is intermediate between the canonical relaxor  $\text{PbMg}_{1/3}\text{Nb}_{2/3}\text{O}_3$  on one hand and lead-free weakly coupled relaxors based on  $\text{BaTiO}_3$  on the other. With the conclusion that the cause of dielectric relaxation in  $\text{Bi}_2\text{Ti}_2\text{O}_7$  containing pyrochlores is the temperature-activated hopping of bismuth atoms between six symmetrically equivalent positions<sup>17–21</sup> taken into account, our data suggest the existence of a correlation between hopping of various bismuth ions in  $\text{Bi}_2\text{Ti}_2\text{O}_7$ . The discovered relaxor-like behavior of the  $\text{Bi}_2\text{Ti}_2\text{O}_7$  single crystal makes it a candidate-material for studying aspects of geometric frustration in nonmagnetic systems and their effect on the suppression of long-range ferroelectric order.

#### ■ ASSOCIATED CONTENT

##### Supporting Information

The Supporting Information is available free of charge at <https://pubs.acs.org/doi/10.1021/acs.cgd.9b01220>.

X-ray diffraction patterns of the powdered crystals and single crystal of  $\text{Bi}_2\text{Ti}_2\text{O}_7$  (S1). Temperature dependence of the electrical resistance of  $\text{Bi}_2\text{Ti}_2\text{O}_7$  single crystal (S2). The plots of  $\ln(f)$  vs  $T_{\text{m}}$  and fitting with Arrhenius equation for one (S3) and for two (S4) relaxation processes. (PDF)

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with a lone pair of electrons.<sup>31</sup> Apparently, a similar situation occurs in  $\text{Bi}_2\text{Ti}_2\text{O}_7$  (Figure 4b), in which incoherent Bi off-centering was detected and investigated by reverse Monte Carlo structural analysis using total neutron scattering.<sup>42</sup> The presence of additional disorder in  $\text{Bi}_2\text{Ti}_2\text{O}_7$  arising from incoherent frozen displacements of the  $\text{Bi}^{3+}$  ions is connected with the observed suppression of excess specific heat at low temperature by Melot et al.<sup>32</sup>

By taking into account the concept developed in refs 31,32,  $\text{Bi}_2\text{Ti}_2\text{O}_7$  can be considered in parallel with relaxor ferroelectrics, in particular, with the canonical relaxor  $\text{PbMg}_{1/3}\text{Nb}_{2/3}\text{O}_3$ , in which a long-range ferroelectric order is suppressed by substitutional disorder. The disordered distribution of  $\text{Mg}^{2+}$  and  $\text{Nb}^{5+}$  ions at crystallographically equivalent positions can lead to the appearance in the system of frustrated interactions (ferroelectric and antiferroelectric) between polar nanoregions with a short-range ferroelectric order.  $\text{Bi}_2\text{Ti}_2\text{O}_7$ , on the contrary, is a well-ordered system, and the frustration in it is a consequence of the specific geometry of the crystal lattice (geometric frustration), which is characteristic of the structure of cubic pyrochlore. In both  $\text{Bi}_2\text{Ti}_2\text{O}_7$  and  $\text{PbMg}_{1/3}\text{Nb}_{2/3}\text{O}_3$ , a decrease in temperature does not lead to a transition to a long-range-ordered ferroelectric state, and



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## Notes

The authors declare no competing financial interest.

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